# Superconductivity in orthorhombic NbS 

Bin-Bin Ruan ©, ${ }^{1, *, \dagger}$ Jun-Kun Yi $\odot,{ }^{1,2, *}$ Le-Wei Chen, ${ }^{1,2}$ Menghu Zhou $\odot,{ }^{1}$ Yun-Qing Shi, ${ }^{1,2}$ Qing-Song Yang ©, ${ }^{1,2}$ Ya-Dong Gu, ${ }^{1,2}$ Gen-Fu Chen, ${ }^{1,2}$ and Zhi-An Ren $\odot^{1,2, ~}{ }^{1}$<br>${ }^{1}$ Institute of Physics and Beijing National Laboratory for Condensed Matter Physics, Chinese Academy of Sciences, Beijing 100190, China<br>${ }^{2}$ School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China

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#### Abstract

Compared to the intensively studied niobium dichalcogenides, the physical properties of niobium monosulfide $(\mathrm{NbS})$ have been less explored. Here we report the discovery of bulk superconductivity in orthorhombic NbS ( $o$ NbS ). First-principles results of $o-\mathrm{NbS}$ are also revealed. $o-\mathrm{NbS}$ crystallizes in a MnP-type structure (Pnma) with lattice parameters $a=6.4450(1) \AA, b=3.31770(4) \AA$, and $c=5.8629(1) \AA$. It exhibits type-II superconductivity with a critical temperature $\left(T_{\mathrm{c}}\right)$ of 6.0 K . Bulk superconductivity is confirmed by the magnetization and heat capacity measurements. The upper and lower critical fields are 7.4 T and 13.0 mT , respectively. Specific heat data suggest that $o-\mathrm{NbS}$ is a fully gapped $s$-wave superconductor, with $\Delta_{0} / k_{\mathrm{B}} T_{\mathrm{c}}=1.75$ and $\Delta C_{\mathrm{e}} / \gamma T_{\mathrm{c}}=1.45$, fitting perfectly within the BCS theory. First-principles calculations indicate that the $\mathrm{Nb}-4 d$ states dominate the Fermi level $\left(E_{\mathrm{F}}\right)$, and the density of states (DOS) on $E_{\mathrm{F}}$ is sensitive to niobium vacancies. Different from the quasi-twodimensional $2 H-\mathrm{NbS}_{2}$ and quasi-one-dimensional $\mathrm{Nb}_{3} \mathrm{~S}_{4}$ superconductors, our discovery of superconductivity in three-dimensional $o-\mathrm{NbS}$ provides a different motif for both experimental and theoretical studies.


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## I. INTRODUCTION

Transition-metal dichalcogenides (TMDs) have garnered much attention in recent years. Most of the TMDs consist of weakly bounded van der Waals layers, which not only give rise to charge density waves (CDWs) [1-3] but also enable delicate fabrication of electronic devices [4,5]. When it comes to superconductivity, the group-5 TMDs, basically $T C h_{2}$ ( $T=\mathrm{Nb}, \mathrm{Ta}, C h=\mathrm{S}, \mathrm{Se}$ ), are the primary focus. Intriguing phenomena, including electron-phonon-driven CDWs [6-8], Ising pairing $[9,10]$, orbital-selective multigap superconductivity [11,12], and topological surface states [13], have been observed in $2 \mathrm{H}-\mathrm{Nb}(\mathrm{Se}, \mathrm{S})_{2}$. These findings have also inspired researchers to explore new superconductors in the $\mathrm{Nb}-\mathrm{S}$ and $\mathrm{Nb}-\mathrm{Se}$ systems. In addition to $2 \mathrm{H}-\mathrm{NbS}_{2}$, which exhibits a transition temperature ( $T_{\mathrm{c}}$ ) of 6.2 K [14,15], superconductivity has also been identified in intercalated $\mathrm{NbS}_{2}$ [16] and in $\mathrm{Nb}_{21} \mathrm{~S}_{8}$ [17].

Unlike the other members in the $\mathrm{Nb}-\mathrm{S}$ phase diagram, niobium monosulfide ( NbS ) has rarely been studied. The existence of NbS has been known since 1938 [18], yet its crystal structure remained elusive until Schönberg reported a hexagonal lattice in 1954 [19]. In 1969, another orthorhombic polymorph of NbS was discovered [20]. Hexagonal NbS ( $h$ - NbS ) was found to undergo a reversible phase transition to the high-temperature orthorhombic form $(o-\mathrm{NbS})$ at 1053 K [20]. Despite $o-\mathrm{NbS}$ been known for over 50 years, its physical properties remain largely unexplored. To the best

[^0]of our knowledge, there are only two references mentioning the transport property of $\mathrm{NbS}[21,22]$. In 1954, Hardy and Hulm performed magnetic measurements on a NbS sample (structure not disclosed), in which no superconductivity was detected above 1.28 K [21]. On the contrary, Narayan and Finnemore reported 3.8 K superconductivity in "orthorhombic NbS" [22]. However, the lattice parameters in Ref. [22] significantly deviated (by $17 \%$ ) from previous reports on $o-\mathrm{NbS}$ single crystals [20], casting doubt on the reliability. Furthermore, no information about the phase purity or evidence of bulk superconductivity was provided. Note that there are other superconducting $\mathrm{Nb}-\mathrm{S}$ phases, including $2 \mathrm{H}-\mathrm{NbS}_{2}$ $\left(T_{\mathrm{c}}=6.2 \mathrm{~K}\right)$ [14], $\mathrm{Nb}_{3} \mathrm{~S}_{4}\left(T_{\mathrm{c}}=4.0 \mathrm{~K}\right)$ [23], and $\mathrm{Nb}_{21} \mathrm{~S}_{8}$ $\left(T_{\mathrm{c}}=4.1 \mathrm{~K}\right)$ [17]. Therefore, one should be very careful to rule out potential contamination from these impurities.

From a theoretical point of view, $o-\mathrm{NbS}$ would be an interesting motif to study, should the superconductivity be confirmed. First, different from its low-dimensional relatives $\left(\mathrm{NbS}_{2}, \mathrm{NbS}_{3}\right.$, or $\left.\mathrm{Nb}_{3} \mathrm{~S}_{4}\right)$ [23-25], o- NbS hosts a unique threedimensional crystal structure. Second, NbS is arguably the simplest compound in the $\mathrm{Nb}-\mathrm{S}$ system, making it a favorable candidate for theoretical research. Unexpectedly, no first-principles studies have been reported for such a simple compound. Lucrezi and Heil explored the binary Nb-S system with $a b$ initio predictions, but they somehow omitted $o-\mathrm{NbS}$ [26]. Very recently, An et al. performed density functional theory (DFT) calculations on $h-\mathrm{NbS}$ without mentioning $o$ NbS [27]. Checking major material databases such as the Materials Project [28], Materiae [29], or Atomly [30], one can find over 100 entries of first-principles results for binary $\mathrm{Nb}-\mathrm{S}$ compounds. However, none of these databases includes information about $o-\mathrm{NbS}$. To date, basic knowledge such as the electronic band structure of $o-\mathrm{NbS}$ is still lacking.

In this study, we report the observation of bulk superconductivity at 6.0 K in $o-\mathrm{NbS}$. Superconducting properties are investigated in detail employing electrical, magnetic, and heat transport measurements. Subsequently, the superconducting parameters for $o-\mathrm{NbS}$ are determined. In addition, first-principles calculations reveal the dominant role of the $\mathrm{Nb}-4 d$ states.

## II. METHODS

Polycrystalline samples of $o-\mathrm{NbS}$ were synthesized by solid-state reactions. The starting materials were Nb (powder, Aladdin Reagents, $99.95 \%$ ) and S (powder, Alfa Aesar, $99.999 \%$ ). To prevent the formation of $\mathrm{Nb}_{3} \mathrm{~S}_{4}$ and minimize niobium vacancies, Nb and S were mixed in a molar ratio of 1.05:1. The mixture was pressed into pellets, placed in evacuated quartz tubes, and annealed at 1363 K for 20 hours before cooled down to 1173 K . The quartz tubes were subsequently quenched in ice water to preserve the orthorhombic NbS phase. The products were ground into fine powder, pressed into pellets, and subjected to one more annealing cycle under the same condition. The final products were black and appeared to be stable under ambient conditions. However, given reports of the degradation of $2 \mathrm{H}-\mathrm{NbS}_{2}$ in air [31], o- NbS was kept in high-purity argon before use.

A powder x-ray diffraction (XRD) pattern at room temperature was collected with a PAN-analytical x-ray diffractometer ( $\mathrm{Cu}-\mathrm{K} \alpha$ radiation). The Rietveld refinement of XRD was performed with the GSAS package [32]. Electrical resistivity was measured on a rectangular cut, using a Quantum Design physical property measurement system (PPMS). The standard four-probe technique was applied. The heat capacity was also measured on a PPMS, using the relaxation method. The magnetic properties were measured on a Quantum Design magnetic property measurement system (MPMS). Note that the magnetic fields in this study have been corrected considering the demagnetization factors [33].

DFT calculations were performed using the QUANTUM ESPRESSO (QE) package [34]. The generalized gradient approximation (GGA) and Perdew-Burke-Ernzerhof (PBE) exchange-correlation functionals were applied. The optimized norm-conserving pseudopotentials of Nb and S were chosen [35]. The energy cutoffs for the wave functions were 60 Ry . The crystal structure was fully relaxed until the force on each atom was less than 0.0002 Ry Bohr $^{-1}$. Monkhorst-Pack $k$-point grids of $5 \times 11 \times 5$ and $9 \times 19 \times 9$ were used to calculate the charge densities, and the density of states (DOS), respectively. The calculations were performed without considering the spin-orbit-coupling (SOC) effects because SOC was found to introduce little change to the results.

## III. RESULTS AND DISCUSSIONS

Figure 1 shows the powder XRD pattern of our $o-\mathrm{NbS}$ sample. The pattern was refined based on the orthorhombic NbS structure (Pnma), as determined from single crystals by Kadijk and Jellinek [20]. No $h-\mathrm{NbS}$ phase was detected. The converged refinement parameters $R_{p}=1.93 \%, R_{w p}=$ $2.89 \%$, and $\chi^{2}=3.2$. The refinement results are plotted in Fig. 1. According to the refinement, there is about $1.1 \mathrm{wt} . \%$


FIG. 1. Powder XRD pattern of NbS at room temperature. Solid lines show the Rietveld refinement results. Vertical bars indicate the Bragg positions from $o-\mathrm{NbS}$ and NbO . The asterisks denote peaks from an unidentified impurity. Inset: the crystal structure of $o-\mathrm{NbS}$.
of NbO as the impurity. In addition, there is a tiny amount of unidentified impurity, which could be other, more complex niobium sulfides such as $\mathrm{Nb}_{21} \mathrm{~S}_{8}$ [36] or $\mathrm{Nb}_{14} \mathrm{~S}_{5}$ [37]. The refined cell parameters for $o-\mathrm{NbS}$ are $a=6.4450(1) \AA, b=$ $3.31770(4) \AA$, and $c=5.8629$ (1) $\AA$. Further crystallographic details are provided in Table I.

The crystal structure of $o-\mathrm{NbS}$ is illustrated in the inset of Fig. 1. Both Nb and S atoms are in a distorted octahedral coordination environment, forming an orthorhombic MnP-type lattice. Different from layered $\mathrm{NbS}_{2}$ or quasi-one-dimensional $\mathrm{NbS}_{3}$ [24,25], $o-\mathrm{NbS}$ possesses a unique three-dimensional structure. According to previous reports [20], o-NbS can host niobium vacancies, resulting in compositions represented as $\mathrm{Nb}_{1-\delta} \mathrm{S}(0 \leqslant \delta \leqslant 0.08)$. For $\delta=0$, the lattice parameters are $a=6.446 \AA, b=3.326 \AA$, and $c=5.897 \AA$, while for $\delta=0.08$, they are $a=6.396 \AA, b=3.334 \AA$, and $c=$ $5.845 \AA$ [20]. Our results of the lattice align with the $\delta=0$ case, implying that the niobium vacancies should be nearly zero. The full occupancy of Nb sites is also confirmed by the XRD refinement (Table I).

On the other hand, the DFT calculations give the relaxed lattice parameters as $a=6.4619 \AA, b=3.3557 \AA$, and $c=$ $6.0280 \AA$. These values agree fairly well with the experimental ones, although the relaxed ones are slightly larger (which is common when using GGA functionals).

TABLE I. Crystallographic parameters of $o-\mathrm{NbS}$ from the Rietveld refinement of XRD. Space group Pnma (No. 62), $a=$ $6.4450(1) \AA, b=3.31770(4) \AA, c=5.8629(1) \AA . U_{\text {eq }}$ is one-third of the trace of the $U_{\mathrm{ij}}$ tensor.

| Atom (site) | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(0.01 \AA^{2}\right)$ | Occupancy |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Nb}(4 c)$ | $0.0061(3)$ | 0.25 | $0.2140(1)$ | $1.51(6)$ | $1.0(0)$ |
| $\mathrm{S}(4 c)$ | $0.2247(4)$ | 0.25 | $0.5788(3)$ | $0.47(7)$ | $1.0(0)$ |



FIG. 2. (a) Temperature dependence of electronic resistivity of $o$ NbS under zero magnetic field. Inset: the $T_{\mathrm{c}}$ evolution with magnetic field; the solid lines are fits with the G-L model. (b) Superconducting transitions under different magnetic fields up to 7 T .

The temperature dependence of resistivity ( $\rho$ ) of $o-\mathrm{NbS}$ is presented in Fig. 2(a). As the temperature decreases below 300 K , the resistivity of $o-\mathrm{NbS}$ decreases monotonically, demonstrating a metallic nature. The residual resistivity ratio $[R R R=\rho(300 \mathrm{~K}) / \rho(7 \mathrm{~K})=1.24]$ is rather small, suggesting the existence of atomic disorder. This may result from the intrinsic Nb vacancies in $o-\mathrm{NbS}$, causing local offstoichiometries. The low-temperature region of $\rho(T)$ is shown in Fig. 2(b), revealing a superconducting transition. We determine the onset value of the transition ( $T_{\mathrm{c}}^{\text {onset }}$ ), at which $\rho(T)$ reaches $90 \%$ of the resistance of the normal state; the midpoint of the transition $\left(T_{\mathrm{c}}^{\text {mid. }}\right)$, at which $\rho(T)$ reaches $50 \%$ of the normal state resistance; and $T_{\mathrm{c}}^{\text {zero }}$, at which $\rho(T)$ drops to zero. $T_{\mathrm{c}}^{\text {onset }}, T_{\mathrm{c}}^{\text {mid. }}$, and $T_{\mathrm{c}}^{\text {zero }}$ are thus determined to be 6.0 , 5.5 , and 5.2 K , respectively.

The superconducting transition was suppressed as magnetic fields were applied, as depicted in Fig. 2(b). The evolution of $T_{\mathrm{c}}$ over the magnetic field is shown in the inset of Fig. 2(a). According to the Ginzburg-Landau (G-L) theory, the upper critical field $\left[\mu_{0} H_{\mathrm{c} 2}(T)\right]$ is fitted with $\mu_{0} H_{\mathrm{c} 2}(T)=$ $\mu_{0} H_{\mathrm{c} 2}(0)\left(1-t^{2}\right) /\left(1+t^{2}\right)$, in which $t=T / T_{\mathrm{c}}[38] . \mu_{0} H_{\mathrm{c} 2}(0)$ is determined to be 7.4 T from the $T_{\mathrm{c}}^{\text {onset }}$ curve. In contrast to $2 H-\mathrm{NbS}_{2}$ [39], $o-\mathrm{NbS}$ exhibits no evident signatures of multigap superconductivity [i.e., upward curvature in $\left.\mu_{0} H_{\mathrm{c} 2}(T)\right]$.


FIG. 3. (a) Temperature dependence of DC magnetic susceptibility of $o-\mathrm{NbS}$. Inset: the temperature dependence of lower critical field $\mu_{0} H_{\mathrm{cl}}(T)$. The solid line is a fit with the G-L model. (b) Fielddependent magnetization of $o-\mathrm{NbS}$ at different temperatures below $T_{\mathrm{c}}$. The discontinuous points are due to avalanches caused by flux jump. The dashed line guides the Meissner states.

The superconductivity of $o-\mathrm{NbS}$ was further confirmed by temperature-dependent magnetization measurements. The results are shown in Fig. 3. The demagnetization factor $(N)$ for the rectangular sample (of dimensions $a \times b \times c$ ) was determined by $N=a b /[a b+3 c(a+b) / 4]$ [33]. Both the zero-field-cooled (ZFC) and field-cooled (FC) DC magnetic susceptibility ( $4 \pi \chi$ ) curves exhibit a superconducting transition below 5.4 K , consistent with the $\rho(T)$ results. $T_{\mathrm{c}}$ determined from the intersection of normal state $4 \pi \chi(T)$ and the steepest slope is 4.8 K . The ZFC $4 \pi \chi$ approaches $100 \%$ at 2.0 K , confirming the existence of bulk superconductivity. Figure 3(b) demonstrates the isothermal magnetization [ $M(H)$ ] curves at different temperatures. These curves exhibit behaviors of a typical type-II superconductor. One interesting feature is that the $M(H)$ curves at 2.0 and 2.5 K show discontinuities from flux jumps, which are explained by the adiabatic model [40]. According to this model, when dissipative heat generated by vortex movements is not promptly absorbed, a small thermal fluctuation can eventually trigger avalanchelike heating, which brings part of the superconductor to the normal state. Flux jumps have been frequently observed in Nb -based

TABLE II. Superconducting and thermodynamic parameters of $o-\mathrm{NbS}$.

| Parameter | Unit | Value |
| :--- | :---: | :---: |
| $T_{\mathrm{c}}^{\text {onset }}$ | K | 6.0 |
| $T_{\mathrm{c}}^{\text {zero }}$ | K | 5.2 |
| $\mu_{0} H_{\mathrm{cl}}(0)$ | mT | 13.0 |
| $\mu_{0} H_{\mathrm{c} 2}(0)^{\mathrm{a}}$ | T | 7.4 |
| $\xi_{\mathrm{GL}}$ | nm | 7.5 |
| $\lambda_{\mathrm{GL}}$ | nm | 221.0 |
| $\kappa_{\mathrm{GL}}$ |  | 29.4 |
| $\gamma$ | $\mathrm{~mJ} \mathrm{~mol}^{-1} \mathrm{~K}^{-2}$ | 4.87 |
| $\beta$ | $\mathrm{~mJ} \mathrm{~mol}^{-1} \mathrm{~K}^{-4}$ | 0.060 |
| $\Theta_{\mathrm{D}}$ | K | 402 |
| $\lambda_{\mathrm{ep}}$ |  | 0.59 |
| $\Delta C_{\mathrm{e}} / \gamma T_{\mathrm{c}}$ | $\mathrm{meV}^{2}$ | 1.45 |
| $\Delta_{0}$ | $\mathrm{eV}^{-1} \mathrm{f.u.}^{-1}$ | 0.77 |
| $N\left(E_{\mathrm{F}}\right)$ |  | 1.30 |

${ }^{\text {a }}$ From $T_{\mathrm{c}}^{\text {onset }}$.
alloy superconductors [41], $\mathrm{MgB}_{2}$ [42], and iron-based superconductors [43]. Nevertheless, we can still get the lower critical fields ( $\mu_{0} H_{\mathrm{c} 1}$ ) from the deviations of $M(H)$ from the initial Meissner states. The temperature dependence of $\mu_{0} H_{c 1}$ is summarized in the inset of Fig. 3(a). $\mu_{0} H_{\mathrm{cl}}(T)$ is fitted with the G-L formula [38]: $\mu_{0} H_{\mathrm{c} 1}(T)=\mu_{0} H_{\mathrm{c} 1}(0)\left[1-\left(T / T_{\mathrm{c}}\right)^{2}\right.$ ] (shown as the solid line), yielding an estimated value of $\mu_{0} H_{\mathrm{c} 1}(0)$ to be 13.0 mT .

Gathering results from the resistivity and magnetization measurements, we are able to estimate the basic superconducting parameters of $o-\mathrm{NbS}$. The coherence length ( $\xi_{\mathrm{GL}}$ ) is determined by [38]

$$
\begin{equation*}
\mu_{0} H_{\mathrm{c} 2}(0)=\Phi_{0} /\left(2 \pi \xi_{\mathrm{GL}}^{2}\right) \tag{1}
\end{equation*}
$$

in which $\Phi_{0}$ is the flux quantum. Note that $\mu_{0} H_{c 2}(0)$ in Eq. (1) represents the one determined from $T_{\mathrm{c}}^{\text {zero }}$. The penetration depth ( $\lambda_{\mathrm{GL}}$ ) is calculated by [44]

$$
\begin{equation*}
\mu_{0} H_{\mathrm{cl} 1}(0)=\frac{\Phi_{0}}{4 \pi \lambda_{\mathrm{GL}}^{2}}\left[\ln \left(\kappa_{\mathrm{GL}}\right)+0.5\right] \tag{2}
\end{equation*}
$$

in which $\kappa_{\mathrm{GL}} \equiv \lambda_{\mathrm{GL}} / \xi_{\mathrm{GL}}$ is the G-L parameter. From Eqs. (1) and (2), $\xi_{\mathrm{GL}}, \lambda_{\mathrm{GL}}$, and $\kappa_{\mathrm{GL}}$ are estimated to be 7.5 and 221.0 nm , and 29.4 , respectively. Note that $\kappa_{\mathrm{GL}}$ is obviously larger than $1 / \sqrt{2}$, suggesting type-II superconductivity in $o-\mathrm{NbS}$. In addition, we estimate the thermodynamic field [ $\mu_{0} H_{\mathrm{c}}(0)$ ] to be 0.15 T by $H_{\mathrm{c}}^{2}(0) \ln \kappa_{\mathrm{GL}}=H_{\mathrm{c} 1}(0) H_{\mathrm{c} 2}(0)$. These superconducting parameters are summarized in Table II.

To gain further insight into the superconductivity, we conducted specific heat ( $C_{\mathrm{p}}$ ) measurements on $o-\mathrm{NbS}$, and the results are shown in Fig. 4(a). The $C_{\mathrm{p}}(T)$ curve under zero magnetic field records a pronounced peak below 6.0 K , confirming the bulk superconductivity. Under a field of 8 T , the superconducting transition is completely suppressed. The curve at 8 T is well fitted with the standard Debye model $C_{\mathrm{p}}(T) / T=\gamma+\beta T^{2}$, with $\gamma=4.87 \mathrm{~mJ} \mathrm{~mol}^{-1} \mathrm{~K}^{-2}$ and $\beta=$ $0.060 \mathrm{~mJ} \mathrm{~mol}^{-1} \mathrm{~K}^{-4}$. Consequently, the Debye temperature $\left(\Theta_{\mathrm{D}}\right)$ is estimated to be 402 K by $\Theta_{\mathrm{D}}=\left(12 \pi^{4} N R / 5 \beta\right)^{1 / 3}$, in which $R$ is the ideal gas constant and $N=2$.


FIG. 4. (a) Temperature-dependent specific heat $\left(C_{\mathrm{p}}\right)$ of $o-\mathrm{NbS}$ under zero and 8 T magnetic field. The solid line is a fit with the Debye model. Inset: $C_{\mathrm{p}}(T)$ from 10 to 300 K . (b) Temperaturedependent electronic specific heat ( $C_{\mathrm{e}}$ ) under zero magnetic field. The solid lines are a fit with the $\alpha$ model.

The $C_{\mathrm{p}}(T)$ data from 10 to 300 K under zero magnetic field are presented in the inset of Fig. 4(a). By combining the results from the resistivity [Fig. 2(a)] and specific heat measurements, we conclude that there are no structural phase transitions or CDW orders occurring below 300 K .

We further obtained the electronic specific heat $\left(C_{\mathrm{e}}\right)$ by subtracting the phononic terms [Fig. 4(b)]. $T_{\mathrm{c}}$ estimated from $C_{\mathrm{e}}(T)$ is 5.1 K , which reasonably agrees with the values from the resistivity and magnetization measurements. $C_{\mathrm{e}}(T)$ in the superconducting state is fitted with the $\alpha$ model [45], in which the entropy

$$
\begin{equation*}
S(T)=-\frac{6 \gamma}{\pi^{2} k_{\mathrm{B}}} \int_{0}^{\infty}[f \ln f+(1-f) \ln (1-f)] \mathrm{d} \epsilon \tag{3}
\end{equation*}
$$

$f=1 /\left\{1+\exp \left[\sqrt{\epsilon^{2}+\Delta^{2}(T)} / k_{\mathrm{B}} T\right]\right\}$, and the isotropic gap function $\Delta(T)=\Delta_{0} \tanh \left\{1.82\left[1.018\left(T_{\mathrm{c}} / T-1\right)\right]^{0.51}\right\} \quad\left(k_{\mathrm{B}}\right.$ is the Boltzmann constant). As shown in Fig. 4(b), the experimental data are well described by the $\alpha$ model, implying $o-\mathrm{NbS}$ possibly to be an $s$-wave superconductor. Additionally, the zero-temperature superconducting gap $\left(\Delta_{0}\right)$ is fitted to be 0.77 meV . Both the coupling strength $\left(\Delta_{0} / k_{\mathrm{B}} T_{\mathrm{c}}=1.75\right)$ and the normalized $C_{\mathrm{e}}$ jump $\left(\Delta C_{\mathrm{e}} / \gamma T_{\mathrm{c}}=1.45\right)$ perfectly agree


FIG. 5. (a) DFT electronic band structure of $o-\mathrm{NbS}$ without SOC near the Fermi level $\left(E_{\mathrm{F}}\right)$. (b) Calculated DOS of $o-\mathrm{NbS}$ near $E_{\mathrm{F}}$. The $E_{\mathrm{F}}$ window for $o-\mathrm{Nb}_{1-\delta} \mathrm{S}(0 \leqslant \delta \leqslant 0.08)$ is also plotted.
with the Bardeen-Cooper-Schrieffer (BCS) weak-coupling ratios (1.76 and 1.43, respectively) [46].

The electron-phonon coupling constant $\lambda_{\text {ep }}$ is estimated by the McMillan relation [47],

$$
\begin{equation*}
\lambda_{\mathrm{ep}}=\frac{1.04+\mu^{*} \ln \left(\Theta_{\mathrm{D}} / 1.45 T_{\mathrm{c}}\right)}{\left(1-0.62 \mu^{*}\right) \ln \left(\Theta_{\mathrm{D}} / 1.45 T_{\mathrm{c}}\right)-1.04} \tag{4}
\end{equation*}
$$

where $\mu^{*}$ is the Coulomb pseudopotential parameter. For $\mu^{*}=0.13, \lambda_{\text {ep }}=0.59$ is obtained, again suggesting weak electron-phonon coupling. Based on the values of $\gamma$ and $\lambda_{\mathrm{ep}}$, the DOS at the Fermi level $N\left(E_{\mathrm{F}}\right)=3 \gamma /\left[\pi^{2} k_{\mathrm{B}}^{2}\left(1+\lambda_{\text {ep }}\right)\right]=$ 1.30 states $\mathrm{eV}^{-1}$ per formula unit (f.u.).

Figure 5 summarizes the calculated electronic band structures and DOS near the Fermi level $\left(E_{\mathrm{F}}\right)$. The $k$-path labels are from the SEEK-PATH code [48]. Multiple bands cross $E_{\mathrm{F}}$, confirming the metallic nature of $o-\mathrm{NbS}$. Most of the bands show relatively large energy dispersion, implying that the correlation effects might be insignificant. As shown in Fig. 5(b), the states near $E_{\mathrm{F}}$ are dominated by the Nb electrons, with minor contributions from S . Most of the Nb states originate from $\mathrm{Nb}-4 d$ orbitals, while the S states are mainly from $\mathrm{S}-3 p$. Note that $E_{\mathrm{F}}$ of stoichiometric $o-\mathrm{NbS}$ locates at a sharp peak on the DOS curve. And the DOS value reads 1.59 states $\mathrm{eV}^{-1}$ f.u. ${ }^{-1}$ at $E_{\mathrm{F}}$. At first glance, this value differs from the experimental $N\left(E_{\mathrm{F}}\right)\left(1.30\right.$ states $\mathrm{eV}^{-1}$ f.u. $\left.{ }^{-1}\right)$. However, when considering the Nb vacancies, DOS at $E_{\mathrm{F}}$ is expected to be lower. Figure 5(b) shows the window of $E_{\mathrm{F}}$ of $o-\mathrm{Nb}_{1-\delta} \mathrm{S}(0 \leqslant$ $\delta \leqslant 0.08$ ) assuming a rigid band. DOS on $E_{\mathrm{F}}$ will drastically reduce to 1.35 states $\mathrm{eV}^{-1}$ f.u. ${ }^{-1}$ even when $\delta=0.005$.

Such sensitivity of $N\left(E_{\mathrm{F}}\right)$ to small changes in niobium vacancies may explain the conflicting results of NbS
properties in previous studies. According to McMillan's formalism [47], $\lambda_{\text {ep }}$ is expressed as $\left[N\left(E_{\mathrm{F}}\right)\left\langle I^{2}\right\rangle\right] /\left[M\left\langle\omega^{2}\right\rangle\right]$, in which $M$ is the atomic mass, and $\left\langle I^{2}\right\rangle$ and $\left\langle\omega^{2}\right\rangle$ stand for average electron-phonon matrix elements, and phonon frequencies, respectively. As $\delta$ in $o-\mathrm{Nb}_{1-\delta} \mathrm{S}$ increases from 0 to $0.08, N\left(E_{\mathrm{F}}\right)$ is reduced from 1.59 to 1.05 states $\mathrm{eV}^{-1}$ f.u. ${ }^{-1}$ [Fig. 5(b)]. Consequently, $T_{\mathrm{c}}$ will be lowered too. The existence of Nb vacancies leads to an enhancement of defect scattering, which is also damaging to superconductivity. As a result, superconductivity fades with increasing $\delta$. This could be the reason why Hardy et al. failed to observe superconductivity above 1.28 K [21], and why Narayan et al. reported a much lower $T_{\mathrm{c}}(3.8 \mathrm{~K})$ [22]. Neither of the previous studies on NbS provided sufficient information regarding the lattice parameters, so it is hard to estimate the Nb vacancies in their samples. Nevertheless, Narayan et al. did notice that $T_{\mathrm{c}}$ "appears to drop with increasing sulfur content" [22], consistent with the above analysis.

Superconductivity in other niobium-based TMDs is similarly sensitive to stoichiometry. For instance, in $2 \mathrm{H}-\mathrm{Nb}_{1+\delta} \mathrm{Se}_{2}$, $T_{\mathrm{c}}$ sharply drops from 7.2 to 2.2 K as $\delta$ increases from 0 to 0.05 [49]. In $2 H-\mathrm{NbS}_{2-y}, T_{\mathrm{c}}$ drops from 6.2 to 2.2 K as $y$ changes from 0 to 0.1 [50]. These studies, together with our present results, emphasize the importance of atomic stoichiometry in the exploration of new niobium-based superconducting materials.

## IV. CONCLUSIONS

In conclusion, we have reported the discovery and detailed investigation of bulk superconductivity in $o-\mathrm{NbS} . o-\mathrm{NbS}$ turns out to be a type-II superconductor with $T_{\mathrm{c}}=6.0 \mathrm{~K}$, and upper and lower critical fields to be 7.4 T and 13.0 mT ,
respectively. The coupling strength $\left(\Delta_{0} / k_{\mathrm{B}} T_{\mathrm{c}}=1.75\right)$ and normalized $C_{\mathrm{e}}$ change ( $\Delta C_{\mathrm{e}} / \gamma T_{\mathrm{c}}=1.45$ ) closely match the BCS theory, evidencing weak electron-phonon coupling. We have also reported the DFT results of $o-\mathrm{NbS}$, from which $E_{\mathrm{F}}$ of stoichiometric $o-\mathrm{NbS}$ is found to locate at a sharp peak on the DOS curve. Different from layered $2 \mathrm{H}-\mathrm{Nb}(\mathrm{S}, \mathrm{Se})_{2}$ superconductors, $o-\mathrm{NbS}$ features a unique three-dimensional MnP-type crystal structure, thus offering a different platform to study the interplay between dimensionality, stoichiometries, and superconductivity in niobium chalcogenide superconductors.

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[^0]:    *These authors contributed equally to this work.
    †bbruan@mail.ustc.edu.cn
    \#renzhian@iphy.ac.cn

